



## Maximizing the Return on Risk-Adjusted Capital: A Performance Perspective Under Solvency II

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# Overview – Research Question & Procedure

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## Research Question

- How does Solvency II influence asset management decisions?
- Which influences have the Solvency II capital requirements on the common performance measure “Return on Risk-Adjusted Capital (RoRAC)”?

## Procedure

1. Starting Point: Construction of a large number of asset portfolios
2. Calculation of the associated capital charges under the Standard Formula
3. Calculation of the insurer’s profit and the resulting RoRAC

# Empirical Data

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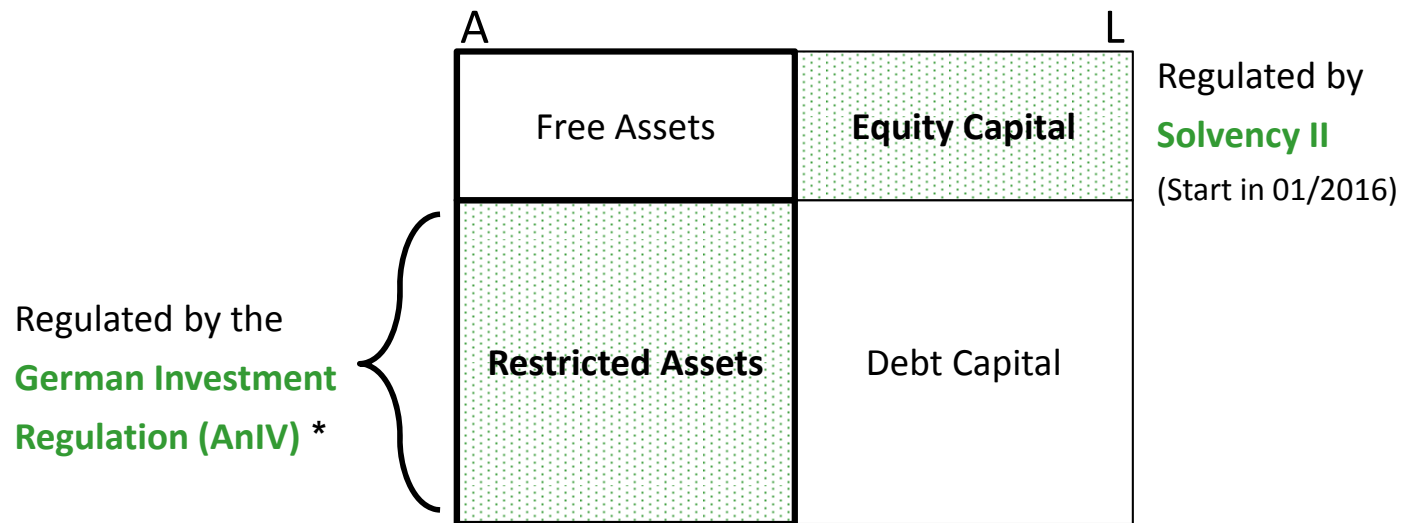
## Three asset classes

- Discrete returns for 25-year period from 07/1990 until 12/2014

Stocks	▪ EURO STOXX 50 Total Return Index
Government Bonds	▪ German Stock Exchange REX Performance Index (REXP)
Real Estate	▪ Real Estate “Grundbesitz” Europa Fund (adjusted for dividends)

Stocks	Expected Return (percent): 8.67 Standard Deviation (percent): 18.48
Government Bonds	Expected Return (percent): 6.20 Standard Deviation (percent): 3.28
Real Estate	Expected Return (percent): 5.03 Standard Deviation (percent): 1.67

# Investment Limits under the German Investment Regulation (AnIV)



*Investment Limits:	Stocks:	20%
	Government Bonds:	none
	Real Estate:	25%

# Construction of Asset Portfolios (1/2)

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## Criteria

- Budget Constraint (portfolio)
- Short-Sale Constraints (asset class)
- Investment Limits Constraint according to AnIV (asset class)

## Procedure

- Discrete increment of 0.1 percent (fixed)
- Open up tree with government bonds
- Insert stocks and real estate sub-portfolios

# Construction of Asset Portfolios (2/2)

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## Government Bonds

## Stocks

## Real Estate

0.000

0.000

0.000

0.001

0.001

0.001

0.002

0.002

0.002

⋮

⋮

⋮

1.000

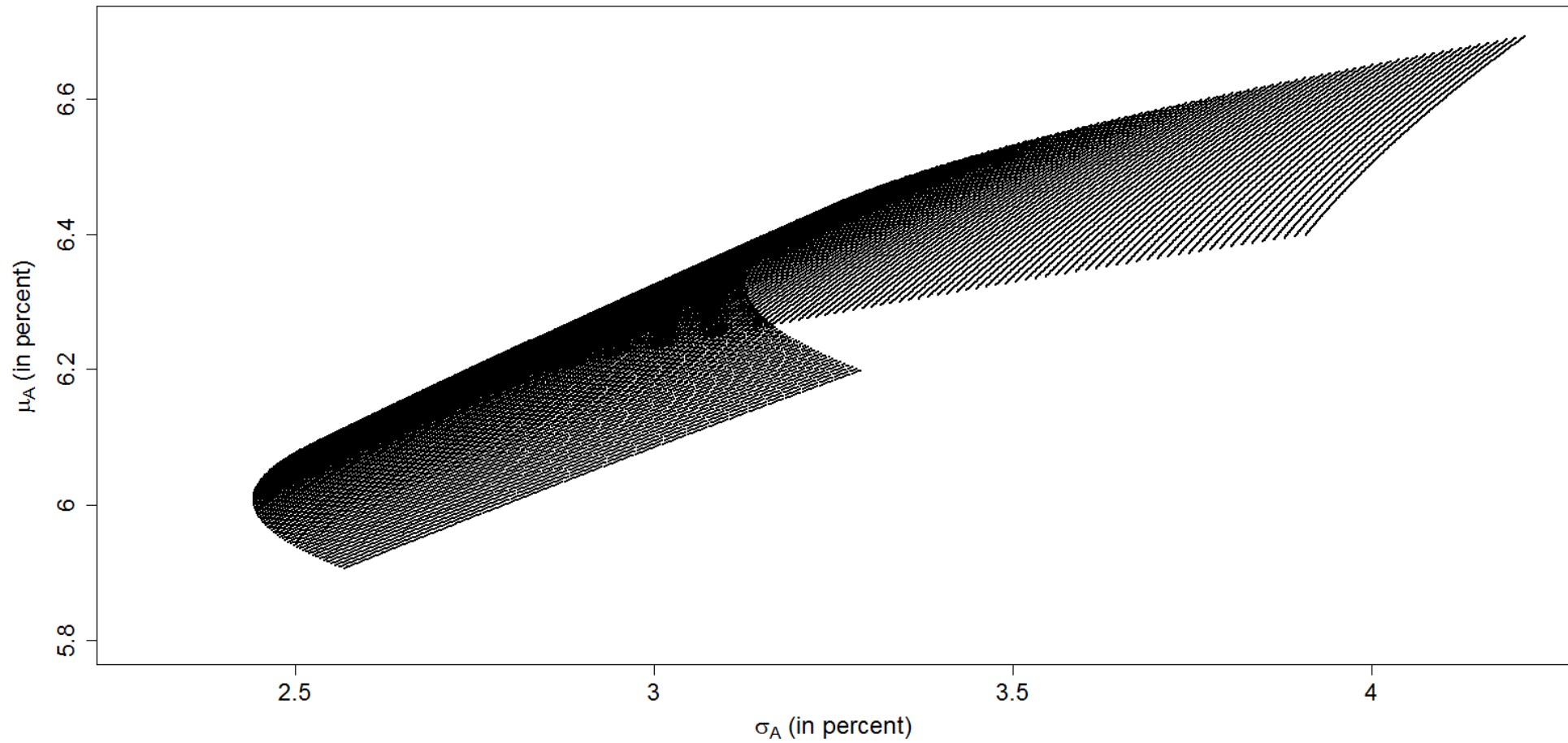
0.200

0.250

- Max. # of possible combinations: 50,501,451 portfolios
- Reduce matrix to fulfill the budget constraint
- Final # of portfolios: 50,451

# Portfolios in Mean-Variance Space

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# Overview – Solvency II

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- Solvency II (01/2016) as new regulatory framework for European insurers:
  - Protection of the policyholders
  - Uniform standards within European insurance landscape
  - Uniform supervisory practice in Europe
- Three-Pillar approach (as Basel II)
- “Two level approach”
  - Definition of minimum capital requirement
  - Definition of Solvency capital requirement (standard formula)



# Solvency II Standard Formula – Market Risk Module

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- Divided into modules (market, health, default, life, non-life, intangibles)
- Market risk accounts for approx. 70 percent of life insurer's capital charges (Fitch, 2011)
- Market risk divided into seven sub-modules: interest rate, equity, property, spread, currency, concentration, illiquidity

## Interest Rate Risk

## Equity

## Property

- In respect to the modelling setup of the standard model, please cf. the paper version

# Simplified Insurance Company (1/2)

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## Assets

Aggregated portfolio return:

$$\tilde{r}_p = (w_1, w_2, w_3) \begin{pmatrix} \tilde{r}_1 \\ \tilde{r}_2 \\ \tilde{r}_3 \end{pmatrix} = \mathbf{w}' \mathbf{R}$$

Assets at the end of the period:

$$\tilde{A}_1 = A_0 \cdot (1 + \tilde{r}_p)$$

## Liabilities

Liabilities at the end of the period:

$$\tilde{L}_1 = L_0 \cdot (1 + \tilde{r}_l)$$

# Simplified Insurance Company (2/2)

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## Equity Capital

Equity capital at the end of the period:  $\widetilde{EC}_1 = (\widetilde{A}_1 - \widetilde{L}_1, 0)^+$

## Profit

Change in the equity capital:

$$\begin{aligned}\tilde{P} &= \widetilde{EC}_1 - EC_0 \\ &= \widetilde{A}_1 - \widetilde{L}_1 - (A_0 - L_0) \\ &= A_0 \cdot \tilde{r}_p - L_0 \cdot \tilde{r}_l \\ &= (\widetilde{EC}_1 - EC_0, -EC_0)^+\end{aligned}$$

- Balance sheet total: **EUR 10 bn**, equity: **12 percent**,  $D_L$ : **10**,  $\tilde{r}_l$ : **1.75 percent**

# Risk-Adjusted Performance Measurement

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- Business activities associated with risks
- ROE as well as ROI, however, based on book values
- The higher the risk of a business activity, the higher the SCR as demanded by Solvency II
- Return on Risk-Adjusted Capital (RoRAC) defined as :

$$RoRAC = \frac{E(\tilde{P})}{SCR_0}$$

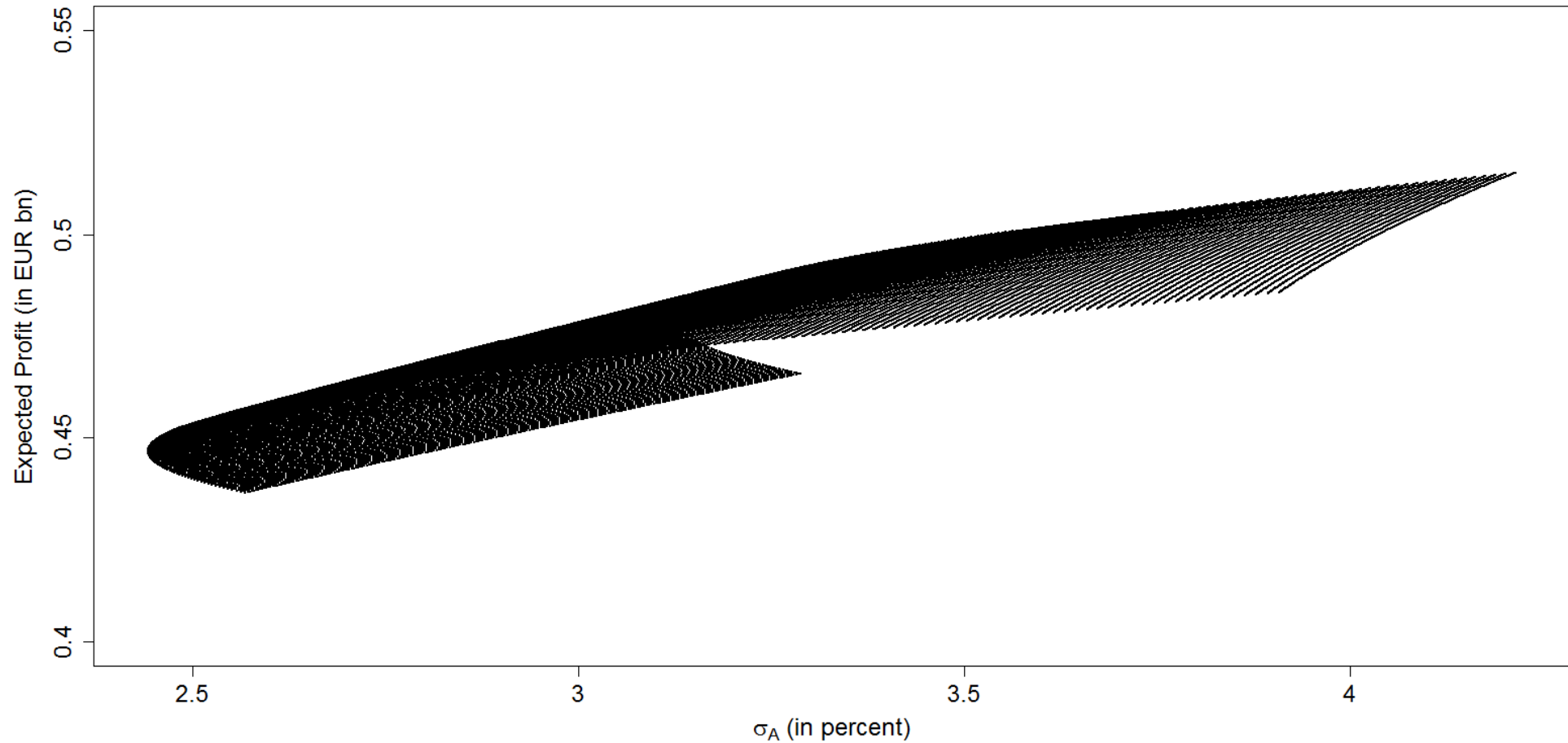
- Insurer can influence the RoRAC by changing the asset allocation
- Process:

Asset-Portfolio ➡ insert in standard model ➡ calculate SCR, E(P) and RoRAC

(for all 50,451 portfolios)

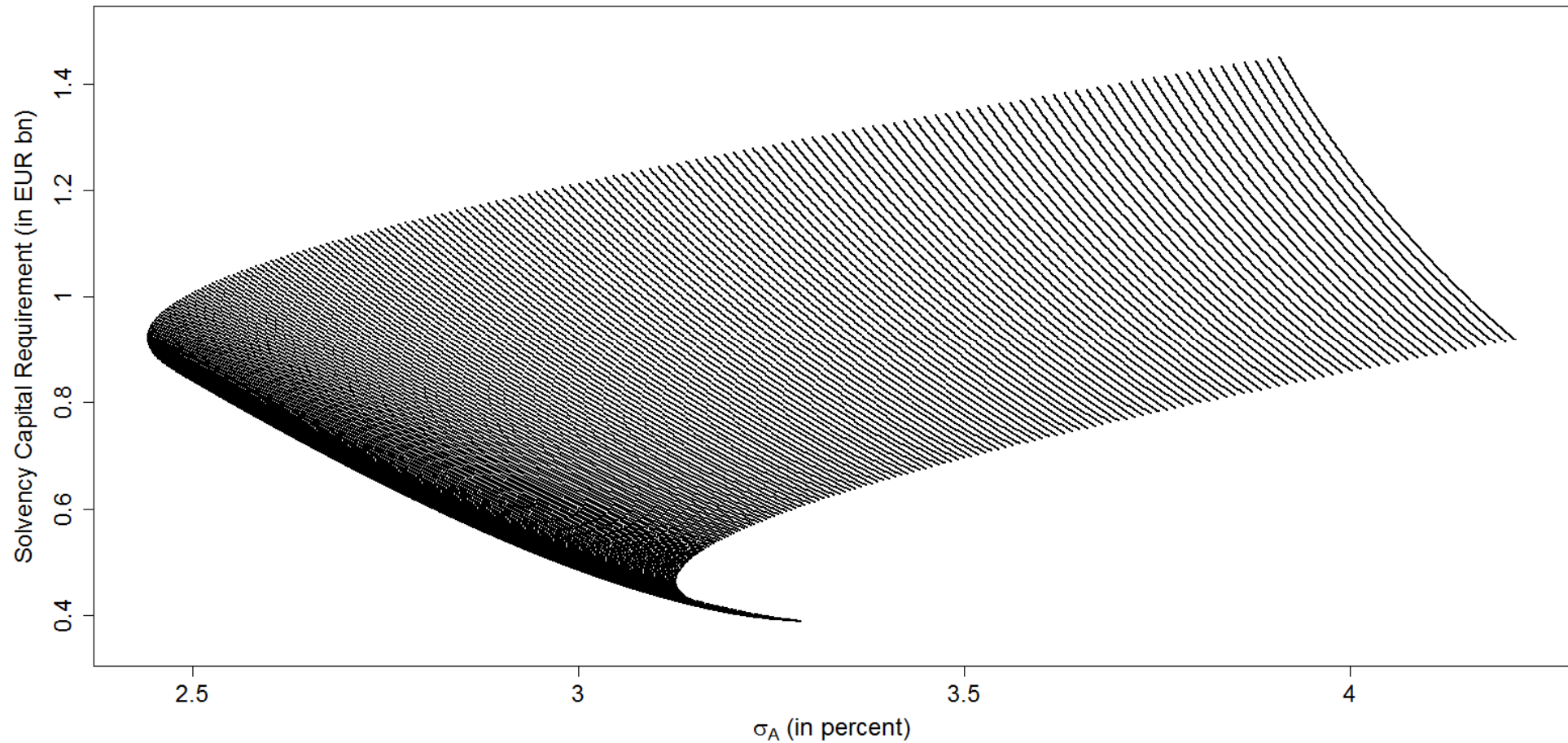
# Results (1/6) – Expected Profit vs. Standard Deviation

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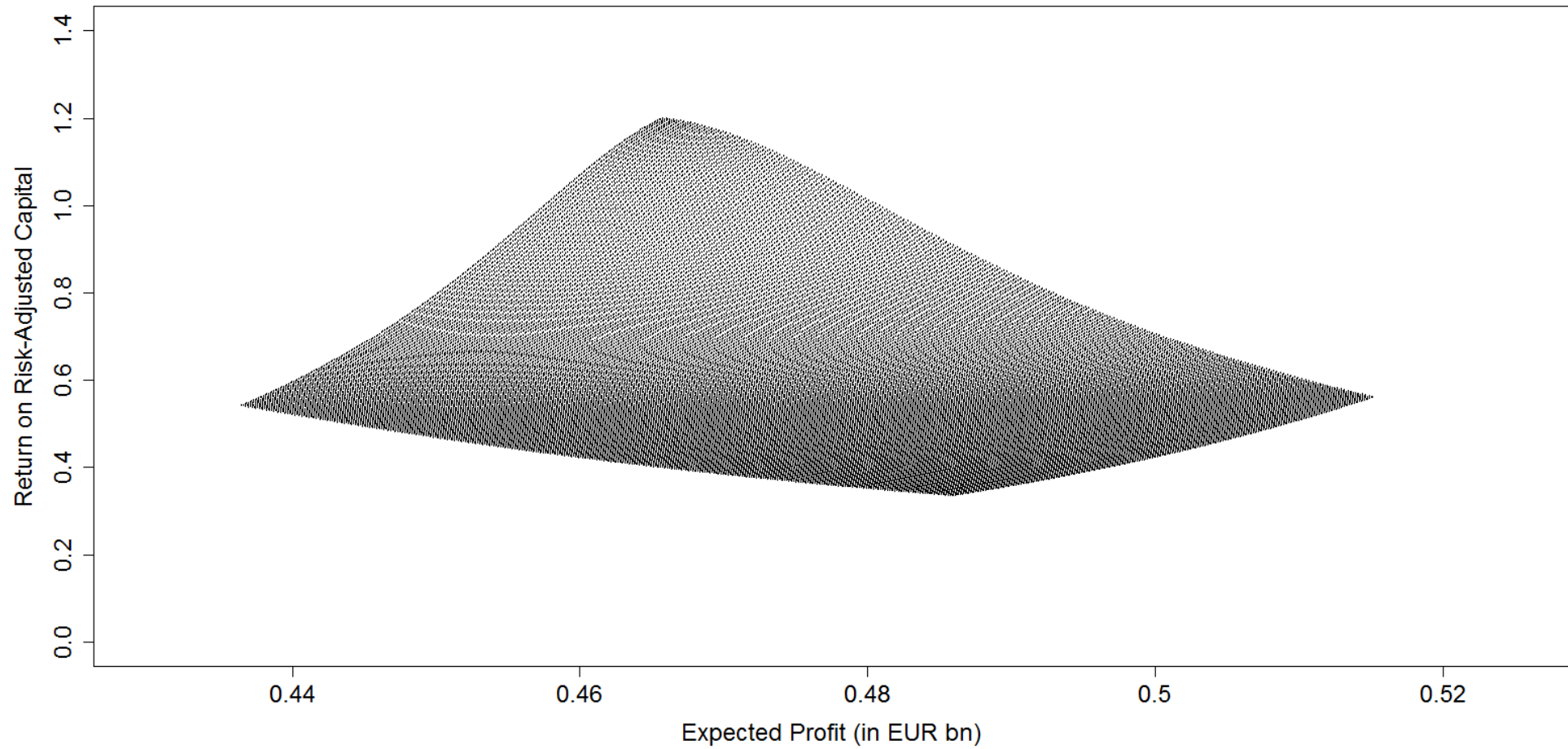
## Results (2/6) – SCR vs. Standard Deviation

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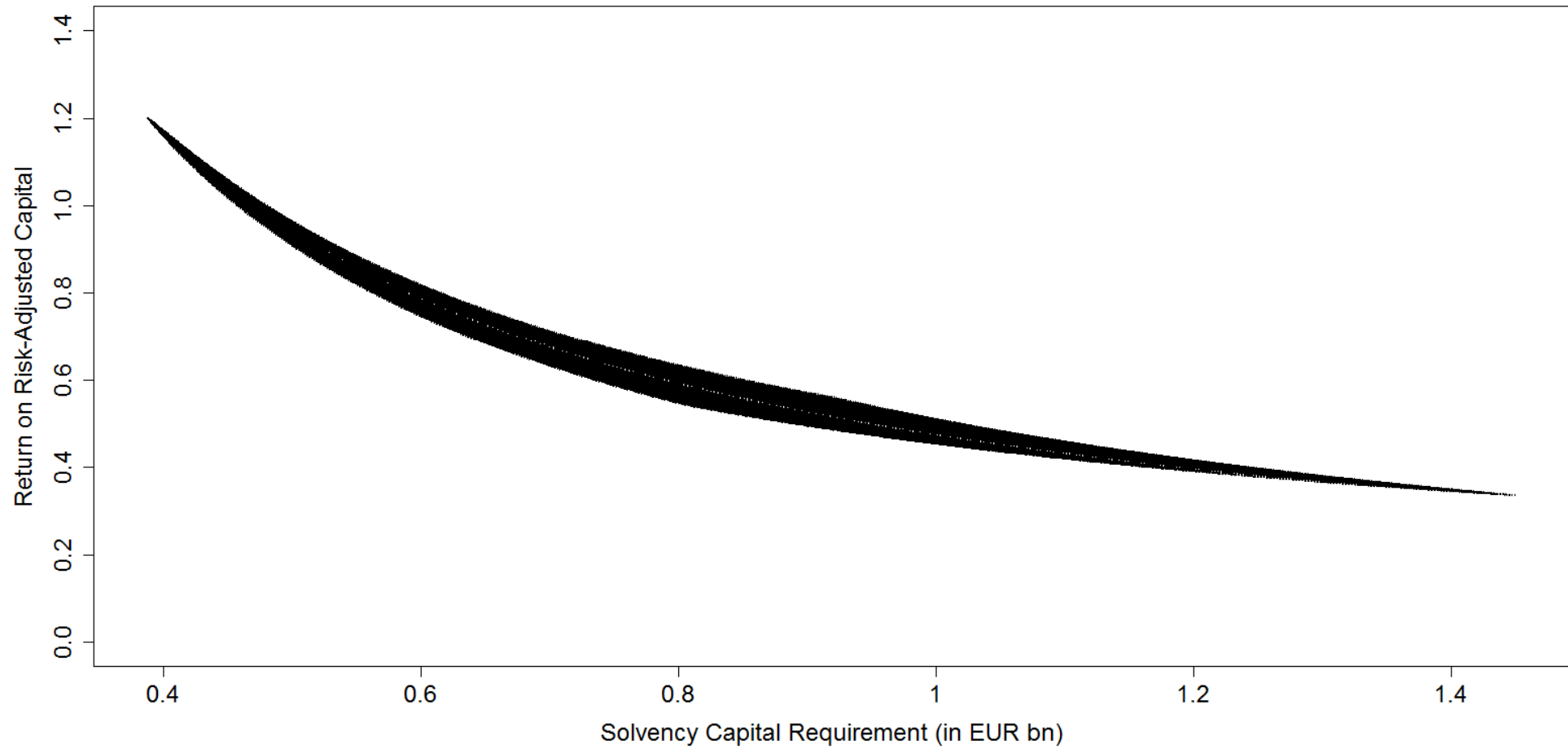
## Results (3/6) – RoRAC vs. Expected Profit

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# Results (4/6) RoRAC vs. SCR

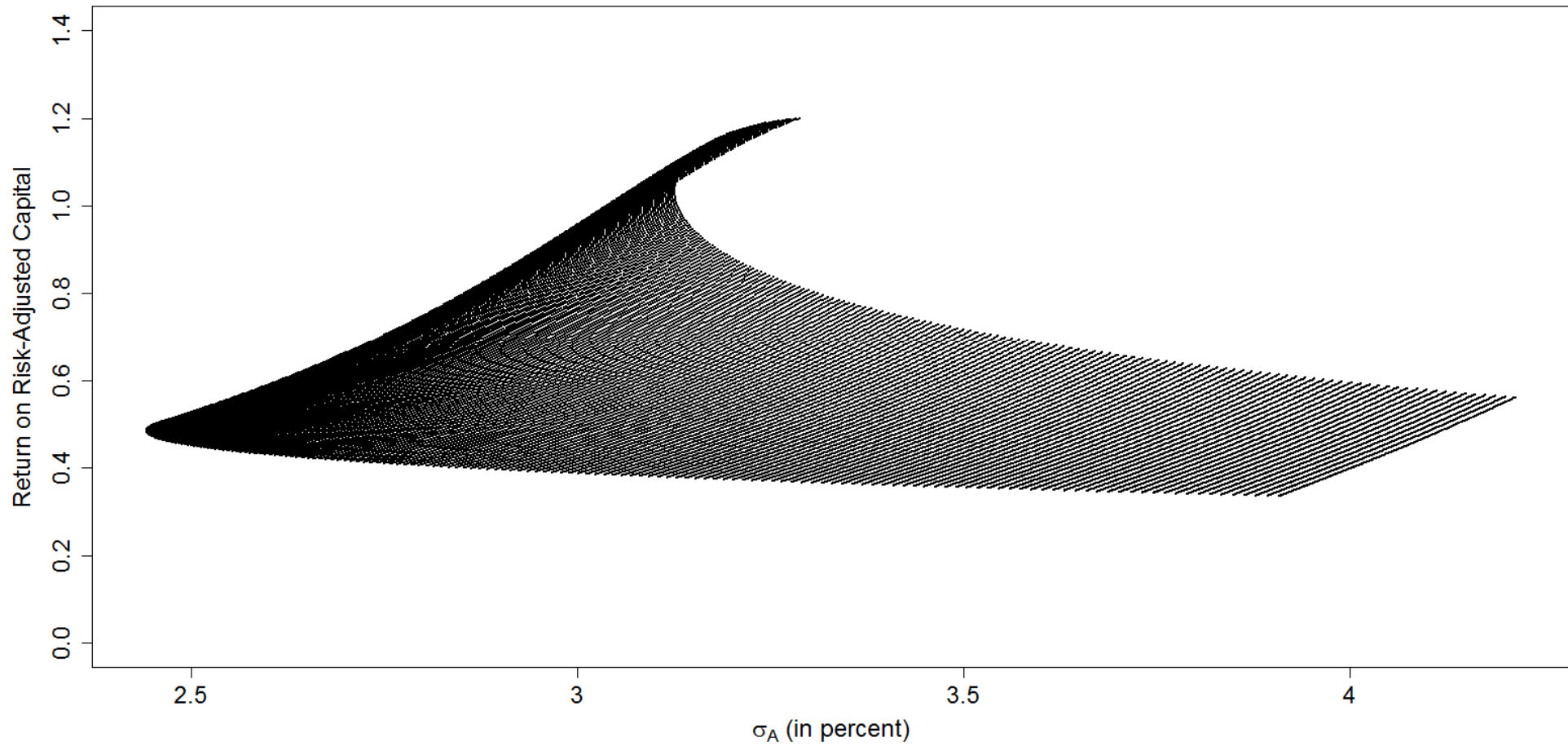
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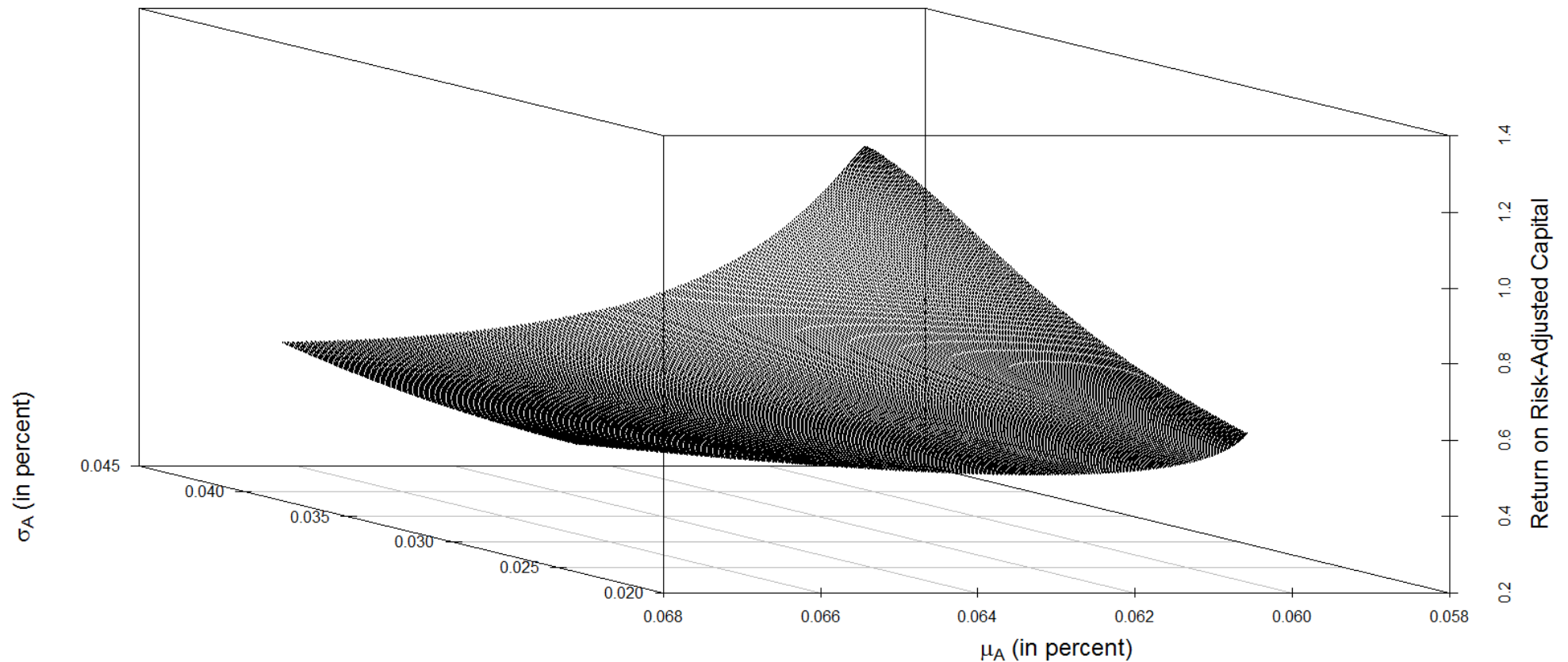


# Results (5/6) – RoRAC vs. Standard Deviation

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# Results (6/6) – RoRAC vs. Standard Deviation vs. Expected Return



# Preliminary Conclusion

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- Profit-maximizing portfolio does not result in the maximum RoRAC
- Portfolio with the lowest SCR achieves the highest RoRAC
- Diversified portfolios lead to low RoRAC figures => SCR as main driver of the RoRAC (increased systemic risk?)

## Next steps in the paper (to do's)

- Extend the # of asset classes in the portfolio to six and run different scenarios (time horizon)
- More detailed analyses of the portfolios: Compare the optimal RoRAC in the standard model with an internal model given  $\varepsilon = 0,5 \%$

=> What are differences in RoRAC and in the portfolio structure / level of SCR?